

Lecture 7: Search 6

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This Lecture

- ♦ RTA*
- ♦ Hierarchical A*
- ♦ Beginning of Local Search
 - Hill-Climbing/Iterative Improvement

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RTA* - Real-Time A*

Intermix partial search with execution of action

- ♦ Goal: reduce the execution time of A*.
- ♦ Method: limit the search horizon of A* and select an action (single move) in constant time.
 - Make decision about *next move in real-world* without a *complete plan* (path) to reach goal state
- ♦ Two stages
 - Make individual move decision: Perform mini-min search with alpha pruning
 - Make a sequence of decisions to arrive at a solution
 - recovering from inappropriate actions
 - avoid loops

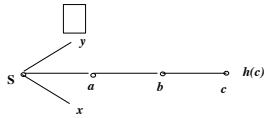
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First Phase - Minimin Search with Alpha-Pruning

- ♦ Mini-min depth-first look-ahead search
 - Returns back-up f value for a node from looking ahead to the frontier node at the horizon
 - *Can viewed as simply a more accurate and computationally expensive heuristic function*
 - Reason: If the heuristic function h is consistent/monotone and admissible, **then the error in the backed-up cost estimate cannot increase with search depth, f is always increasing and thus better estimate of actual cost**
- ♦ Alpha pruning
 - If **current minimum f of horizon node (alpha value)** is less than f of an intermediate node, the intermediate node (and any successors) can be eliminated from further consideration
 - Reason: f is monotonic (*never can get lower f*) and you are only searching to horizon (don't need goal state to prune)

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Basis of RTA*



- ♦ $h(a) \leq g(a \text{ to } c) + h(c) \leq h^*(a)$;
 - assuming you need to go to the goal state thru c from a
- ♦ As a result of exploring in the search space from a to c , you can replace $h(a)$ with the *better (more informed) estimate* $g(a \text{ to } c) + h(c)$
- ♦ This leads to a more informed decision at S whether to take the “action in the real world of moving” to either state y , a , or x .

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Procedure for Calculating Backed-Up Value of a Move

```

procedure evaluate(move, limit)
  /* return backed-up estimate  $f^*$ (move) by  $\alpha$ -pruning search to depth limit */
1. Open  $\leftarrow$  {move};  $\alpha \leftarrow \infty$ 
2.  $f(\text{move}) \leftarrow g(\text{move}) + h(\text{move})$ ;
3. While (open not empty) do
4.   node  $\leftarrow$  pop (Open);
5.   expand node; for each child of node do
6.      $g(\text{child}) \leftarrow g(\text{node}) + \text{move-cost}$ ;
7.      $f(\text{child}) \leftarrow g(\text{child}) + h(\text{child})$ ;
   Prune child if  $f(\text{child}) \geq \alpha$ 
8.     if  $f(\text{child}) < \alpha$  do
9.       if (depth = limit or goal(child)) then
10.         $\alpha \leftarrow f(\text{child})$ ;
11.       else put child on Open; od od od
11. Return  $\alpha$ ;
    
```

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RTA* - Controlling the Sequence of Moves Executed in Real-World

Basic Principle:

“One should backtrack to a *previously visited real world state* when the **estimate of solving the problem from that state plus the cost of returning to that state** is less than the estimated cost of going forward from the current state.” - Korf

- ♦ Merit of every node $f(n) = g(n) + h(n)$ is measured *relative to the current position* of the problem solver in the real-world
 - **initial state is irrelevant**
- ♦ If one moves back to a *previously visited real-world state*, then it needs to take into account that one already has taken action there
 - **value of state is next best f**

Remember Interplay between partial search and execution of action in real-world

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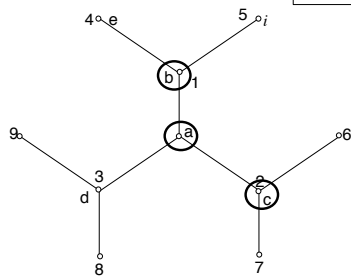
RTA* Algorithm

- ♦ Maintains in a hash table a list of those states/nodes that have been visited by an *actual move* in the real world of the problem solver;
- ♦ At each cycle in the real-world, the current state is expanded and the heuristic function, possibly augmented by look-ahead search, is applied to each successor state which is **not in the hash table**;
- ♦ The f value of each neighboring state is computed by adding the h value plus the cost of the link to the current state;
- ♦ The neighbor with the minimum f value is chosen for the current state;
- ♦ The **second best f value is stored in the hash table** for the current state
 - Represents the estimated h cost of solving the problem by returning to this state
 - Second best avoids loops

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Example of RTA*

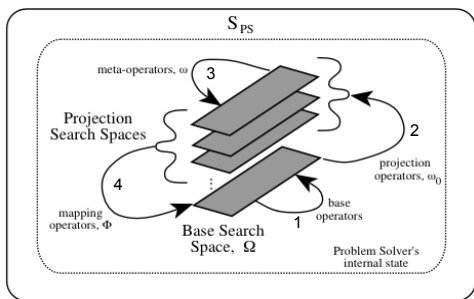
node	h	f
a	3	4
b	5	0
c	2	3
d	3	4
e	4	5
i	5	6



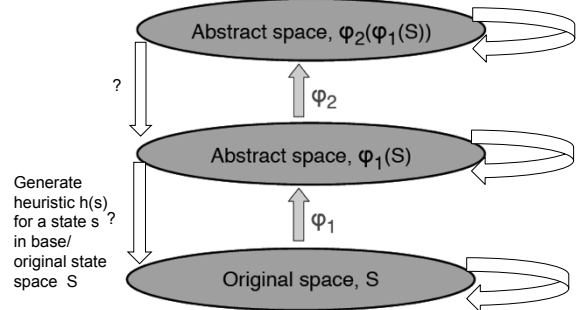
Characteristics of RTA*

- ◆ **Completeness of RTA***
 - In a finite problem space with positive edge costs and finite heuristic value, in which a goal state is reachable from every state, RTA* will find a solution.
- ◆ **Local optimal of RTA***
 - Each move made by RTA* on a tree is along a path whose estimated cost of reaching a goal is minimum, based on the cumulative search frontier at the time.

Hierarchical Problem Solving



Hierarchical Heuristic A* Search

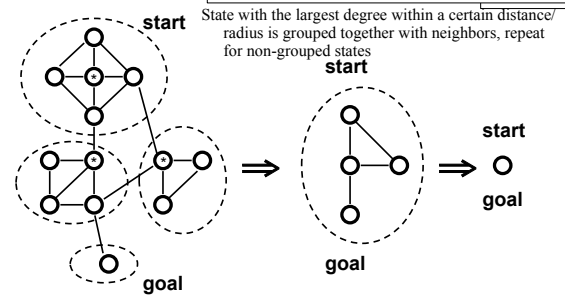


Automatically Generating State Space Abstraction “Max-degree” Star Abstraction

- ◆ The state with the highest degree is grouped together with its neighbors within a certain distance (the abstraction radius) to form a single abstract state.

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Star abstraction with radius = 1



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Naive Hierarchical A*

TABLE I. Naive Hierarchical A* (abstraction radius = 2)

Search Space	Size (# states)		Nodes Expanded		
	All Levels	Base Level	Blind Search	Hierarchical A* All Levels	Hierarchical A* Base Level
Blocks-5	1166	866	389	2766	118
5-puzzle	961	720	348	3119	224
Fool's Disk	4709	4096	1635	12680	629
Hanoi-7	2894	2187	1069	18829	701
KL2000	3107	2736	1236	7059	641
MC 60-40-7	2023	1878	934	2412	702
Permute-6	731	720	286	806	77
Words	5330	4493	1923	19386	604

Naive Hierarchical A* - Cache h in abstract space; avoid search for $h(s_2)$ if $h(s_1)$ already computed [$h(\phi(s_1))$] and $\phi(s_1) = \phi(s_2)$

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Reducing Search in Abstract Spaces

- ◆ Observation: all searches related to the same base level problem have the same goal.
- ◆ This allows additional types of caching of values.
- ◆ It leads to variants of Hierarchical A* Search (Valtorta's barrier) requiring less effort in 5 out of 8 search spaces.

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Exploit Information for Repeated Blind Search in Abstract Space

- ♦ V1 - h*caching
 - Cache exact h's (h*) along optimal solution in abstract space
 - Cache for use in base level search (don't need to search again since already know optimal distant to goal in abstract space) [h($\Phi(s_1)$), h(Φ_1)... h(Φ_p)]
- ♦ V2
 - Cache optimal path in abstract space (optimal-path caching)
 - Exploit in further searches in abstract space (if reach such a node in abstract space can stop search along this path) – can stop further search in Φ once you have h(Φ_p) that you found was on optimal path in previous search
- ♦ V3
 - pertains to states that were opened (or closed) during abstract search but are not on the solution path
 - Remember optimal path length in abstract search space (P-g caching)
 - P being optimal path length from start to goal in abstract space

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Hierarchical A*

TABLE 2. Hierarchical A* (abstraction radius = 2)

Search Space	Blind Search	Nodes Expanded				# problems V3 < BS (out of 200)
		Naive	V1	V2	V3	
Blocks-5	389	2766	1235	478	402	96 *
5-puzzle	348	3119	1616	854	560	14 *
Fool's Disk	1635	12680	8612	3950	1525	132
Hanoi-7	1069	18829	10667	5357	3174	0 *
KL2000	1236	7059	3490	1596	1028	171
MC 60-40-7	934	2412	1531	1154	863	128
Permute-6	286	806	482	279	242	113
Words	1923	19386	7591	2849	1410	124

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The Granularity of Abstraction

- ♦ Increasing the radius of abstraction has two contradictory effects:
 - + **abstract spaces contain fewer states and each abstract search produces values for more states, but**
 - **the heuristic is less discriminating**
- ♦ Using the best case radius Hierarchical A* Search (Valtorta's barrier) is more effective every search space.

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Hierarchical A* with best abstraction radius

TABLE 3. Hierarchical A* (best abstraction radius)

Search Space	Radius	Nodes Expanded			# problems V3 < BS (out of 200)	CPU seconds	
		Blind Search	Naive	Hierarchical A* V3		Blind Search	V3
Blocks-5	5	389	611	309	123	69	86
5-puzzle	12	348	354	340	131	36	40
Fool's Disk	4	1635	1318	1172	194	872	902
Hanoi-7	20	1069	1097	1055	117	102	108
KL2000	5	1236	1306	1072	178	398	384
MC 60-40-7	4	934	822	803	144	266	253
Permute-6	5	286	201	194	192	82	67
Words	3	1923	9184	1356	128	1169	1273

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Local Search

- ◆ In many optimization problems, path is irrelevant (no path cost); the goal state itself is the solution
 - 8-queens problem, job-shop scheduling
 - circuit design, computer configuration
 - automatic programming, automatic graph drawing
- ◆ Then state space = set of “complete” configurations; need to find optimal configuration
- ◆ Can use iterative improvement algorithms; keep single “current” state and try to improve it
 - *Paths followed by search are not retained*
 - Contrast with open and closed node lists; search tree

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Advantages of local search

- ◆ Very simple to implement.
- ◆ Very little memory is needed.
- ◆ Can often find reasonable solutions in very large (*continuous*) state spaces for which systematic algorithms are not suitable.

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Stochastic vs. Systematic Search

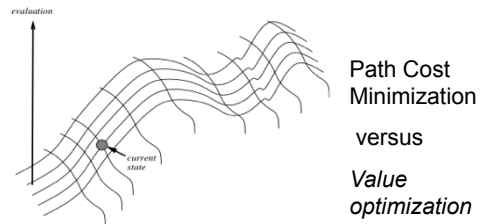
- ◆ Unsolvability -- Is there a solution?
 - Systematic: can require exhaustive examination of exponential search space
 - Stochastic: cannot determine unsolvability
- ◆ Completeness/Optimality
 - Systematic: complete
 - Stochastic: incomplete
- ◆ Speed
 - Neither is uniformly superior; each does better for different sorts of problems

Local Search is an example of Stochastic Search

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Iterative Improvement (*Smart version of Generate & Test*)

- ◆ Start Search with complete but non-optimal solution
- ◆ Modify incorrect/non-optimal solution to move it closer to correct/optimal solution



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Example: Traveling Salesperson Problem

- ♦ Start with any complete tour and perform pair wise exchanges of the end points of two segments



- ♦ Only make change if exchange reduces tour cost
- ♦ Variants of this approach get within 1% of optimal very quickly with thousands of cities

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Next Lecture

- ♦ Continuation of Local Search
 - Hill-Climbing/Iterative Improvement
 - Simulated Annealing (Stochastic Hill Climbing)
 - Beam Search
 - Genetic Algorithm
 - Repair/Debugging (to be done next time)
 - GSAT

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