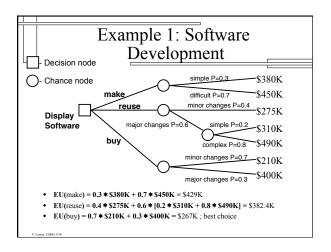
Lecture 21: Uncertainty 6

Victor R. Lesser CMPSCI 683 Fall 2010 Today's Lecture

Decision Trees and Networks

Decision Trees

- A decision tree is an explicit representation of all the possible scenarios from a given state.
- Each path corresponds to decisions made by the agent, actions taken, possible observations, state changes, and a final outcome node.
- Similar to a game played against "nature"

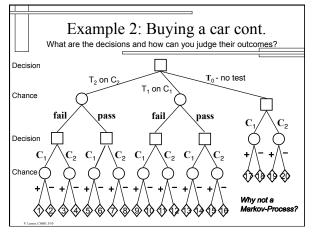


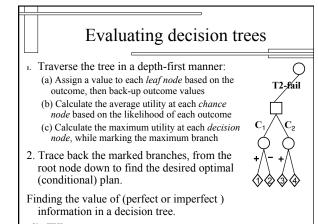
Example 2: Buying a car

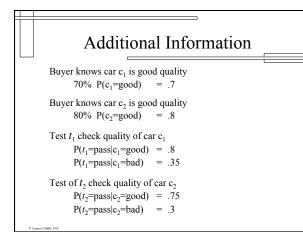
- There are two candidate cars C₁ and C₂, each can be of good quality (+) or bad quality (-).
- + There are two possible tests, T_1 on C_1 (costs \$50) and T_2 on C_2 (costs \$20).
- C₁ costs \$1500 (\$500 below market value) but if it is of bad quality repair cost is \$700.
 500 gain or 200 lost
- C₂ costs \$1150 (\$250 below market value) but if it is of bad quality repair cost is \$150.
 - 250 gain or 100 gain
- Buyer must buy one of the cars and can perform at most one test. -- What other information?

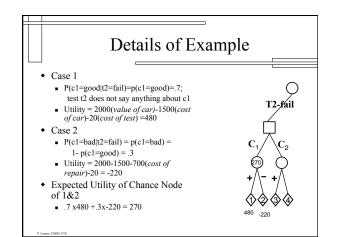
Example 2: Buying a car cont.

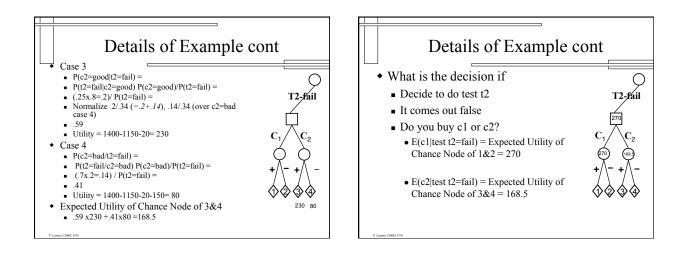
- The chances that the cars are of good quality are 0.70 for C_1 and 0.80 for C_2 .
- Test T₁ on C₁ will confirm good quality with probability 0.80 if C₁=good and will confirm bad quality with probability 0.65 if C₁= bad.
 Imperfect information
- Test T₂ on C₂ will confirm good quality with probability 0.75 and will confirm bad quality with probability 0.70.

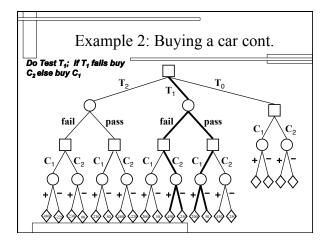










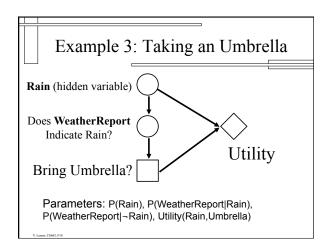


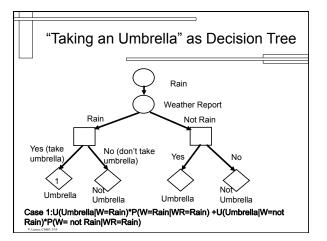
Decision Networks/Influence Diagrams

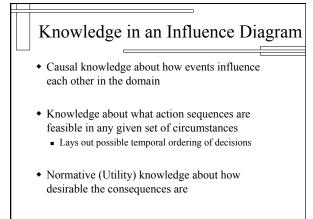
- Decision networks or influence diagrams are an extension of belief networks that allow for reasoning about actions and utility.
- The network represents information about the agent's current state, its possible actions, the possible outcome of those actions, and their utility.

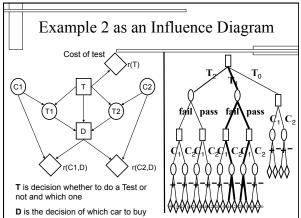
Nodes in a Decision Network

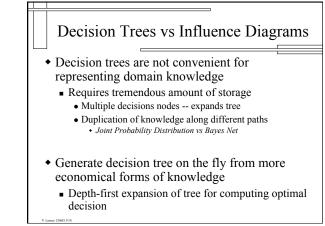
- Chance nodes (ovals) have CPTs (conditional probability tables) that depend on the states of the parent nodes (chance or decision).
- Decision nodes (squares) represent options available to the decision maker.
- Utility nodes (**Diamonds**) or value nodes represent the overall utility *based on the states of the parent nodes*.









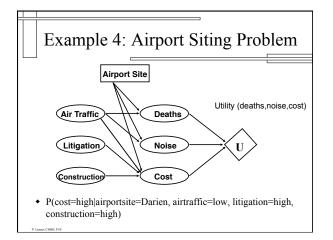


Topology of decision networks

- 1. The directed graph has no cycles.
- 2. The utility nodes have no children.
- 3. There is a directed path that contains all of the decision nodes.
- 4. A CPT is attached to each chance node specifying P(A|parents(A)).
- 5. A real valued function over parents(U) is attached to each utility node.

Semantics

- Links into decision nodes are called "information links," and they
 indicate that the state of the parent is known prior to the decision.
- The directed path that goes through all the decision nodes defines a temporal sequence of decisions.
- It also partitions the chance variables into sets: I₀ is the vars observed before any decision is made, I₁ is the vars observed after the first and before the second decision, etc. I_n is the set of unobserved vars.
- The "no-forgetting" assumption is that the decision maker remembers all past observations and decisions. -- Non Markov Assumption



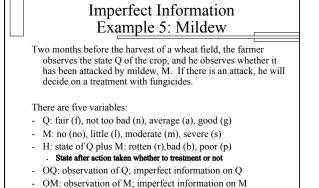
Evaluating Decision Networks

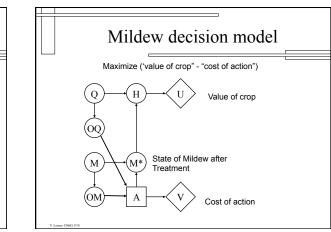
- 1. Set the evidence variables for the current state.
- 2. For each possible value of the decision node(s):(a) Set the decision node to that value.(b) Calculate the posterior probabilities for the parent nodes of the utility node.

(c) Calculate the expected utility for the action.

3. Return the action/decision with the highest utility.

Similar to Cutset Conditioning of a Multiply Connected Belief Network



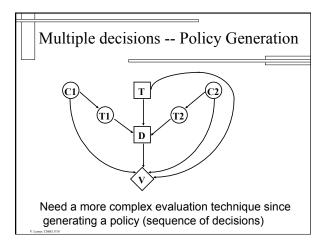


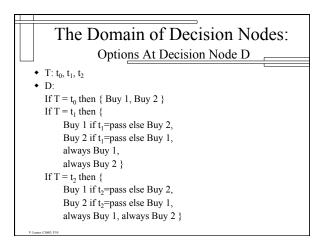
One action in general

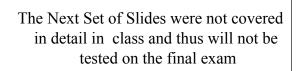
- A single decision node *D* may have links to some chance nodes.
- A set of utility functions $U_1, ..., U_n$ over domains $X_1, ..., X_n$.
- Goal: find the decision d that maximizes EU(D=d | e):

$$EU(D \mid e) = \sum_{X_1} U_1(X_1)P(X_1 \mid D, e) + \dots + \sum_{X_n} U_n(X_n)P(X_n \mid D, e)$$

• How to solve such problems using a standard Bayesian network package?







Evaluation by Graph Reduction

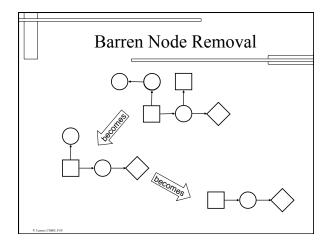
<u>Basic idea</u>: (Ross Shachter) Perform a sequence of transformations to the diagram that preserve the optimal policy and its value, until only the UTILITY node remains.
 Similar to ideas of transformation into polytree

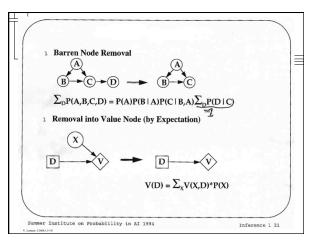
Four basic value/utility-preserving reductions:

- Barren node removal
- Chance node removal (marginalization)
- Decision node removal (maximization)
- Arc reversal (Bayes' rule)

Barren node reduction

- Let X_j represent a subset of nodes of interest in an influence diagram.
- Let *X_k* represent a subset of evidence nodes.
- We are interested in $P(f(X_i) | X_k)$
- A node is "barren" if it has no successors and it is not a member of X_i or X_k .
- The elimination of barren nodes does not affect the value of $P(f(X_i) | X_k)$





Notation for Shachter's algorithm

For chance nodes:

- S(i) = direct successors = children
- C(i) = conditional predecessors = parents
- For decision nodes
- I(i) = information predecessors = parents

