Learning Quantitative Knowledge for Multiagent Coordination

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Abstract

A central challenge of multiagent coordination is reasoning about how the actions of one agent affect the actions of another. Knowledge of these interrelationships can help coordinate agents — preventing conflicts and exploiting beneficial relationships among actions. We explore three interlocking methods that learn quantitative knowledge of such non-local effects in TÆMS, a well-developed framework for multiagent coordination. The surprising simplicity and effectiveness of these methods demonstrates how agents can learn domain-specific knowledge quickly, extending the utility of coordination frameworks that explicitly represent coordination knowledge.

Introduction

A major challenge of designing effective multiagent systems is managing non-local effects — situations where the actions of one agent impact the performance of other agents' actions. For example, one agent's action can enable, disable, facilitate, or hinder the actions of other agents. Poor accounting for these non-local effects (NLEs) can cause multiagent activities to deadlock or waste resources, so representing and reasoning about NLEs is a central feature of frameworks for multiagent coordination (Decker and Lesser 1995; Barbuceanu and Fox 1995).

Multiagent coordination frameworks often assume that agents possess accurate knowledge of the relationships among actions and the basic performance characteristics of those actions (e.g., cost and duration). Such knowledge allows agents to schedule activities in ways that exploit beneficial relationships, and avoid pathological ones. Unfortunately, accurate knowledge of NLEs is difficult to maintain in heterogeneous and open systems. Agent designers may not know the future operating environment for their agents, the complete set of actions open to other agents, and the effects those actions have on their own agents. For all of these reasons, the ability for multiagent systems to autonomously learn coordination knowledge appears critical for next-generation coordination frameworks (Sugawara and Lesser 1998).

We investigated and implemented techniques to learn the statistical knowledge about NLEs represented in one well-established framework for multiagent coordination (TÆMS). We found that a combination of three simple learning techniques can be surprisingly effective. The learned knowledge can be used to accurately predict the performance of a particular action, given its context within a set of actions executed by the same agent or other agents. The success of these methods demonstrates how coordination knowledge can be learned explicitly, as opposed to learning coordination policies that implicitly represent knowledge of agents, environments, and their association.

Context

Learning for multiagent coordination has become a popular topic in the past several years. Much of the existing work aims to equip agents with effective policies — functions that map environmental conditions directly to coordinated actions. For example, Weiß (Weiß 1998) investigates reinforcement learning (RL) techniques to improve the coordinated performance of *reactive* agents. Similarly, Tan (Tan 1998) investigates how to extend RL to create coordinated multiagent policies.

In contrast, we explore learning explicit quantitative knowledge needed by *deliberative* agents — agents that explicitly plan sequences of actions and that can trace the assumptions embedded in those plans. We assume that the coordination framework (TÆMS in this case) encodes all relevant characteristics of the environment needed to guide coordination and that agents can use this knowledge to devise coordinated actions. Separating knowledge from coordination mechanisms provides opportunities (e.g., the coordination strategy can be changed without altering the knowledge), as well as costs (e.g., using the knowledge requires explicit reasoning).

Another theme of learning for multiagent coordination has been learning to predict the future actions of other agents. Such predictions can help produce coordinated actions even without explicit communication among agents. Hu and Wellman (Hu and Wellman 1998) study this type of learning in the context of a simulated double auction. Similarly, Zeng and Sycara (Zeng and Sycara 1997) study learning to predict agent actions in the context of sequential negotiation. In contrast, we focus on learning how agent actions affect each other. While some of this knowledge could be used to predict the reasoning of other agents, it does not directly predict their actions.

Some of the work closest to our own focuses on learning the effects of environmental context on the outcomes of agent actions. For example, Schmill, Rosenstein, Cohen, and Utgoff (Schmill *et al.* 1998) use decision trees to learn the environmental states and actions that produce changes in particular sensor values of a mobile robot. Similarly, Haigh and Veloso (Haigh and Veloso 1998) learn situation-dependent costs of actions from execution traces of robot navigation. This work and other similar work focuses on the relationships among actions and outcomes, a notion closely allied with our focus on actions and their non-local effects (NLEs) in a multiagent context. However, the "environment" in our work consists almost entirely of the actions of other agents, and the desired knowledge concerns how to coordinate the actions of multiple agents.

Tasks

We investigated learning techniques for TÆMS, an existing framework for multiagent coordination. TÆMS (Decker and Lesser 1993) represents quantitative information about agent activities, including candidate actions and how those actions can combine to achieve high-level tasks. TÆMS represents a task as a tree whose root is the overall task and whose leaves are primitive actions referred to as *methods*. Internal nodes represent subtasks composed of other tasks and methods. Internal nodes also specify how the constituent methods and tasks combine for successful execution (e.g., all must execute successfully, or only a single alternative must execute successfully). In addition to this structural information about tasks and methods, TÆMS represents two types of statistical information — 1) probability distributions that describe the possible values of performance parameters of a method (e.g., the quality of a method's result, the cost of the method, and its duration); and 2) non-local effects (NLEs) of one method on another (e.g., enables, disables, facilitates, and hinders).

Reasoners can use the knowledge represented in TÆMS (Wagner *et al.* 1998a) to evaluate the quality, cost, and duration of possible courses of action and their effects on other agent's actions. Using this information, reasoners can select the one that best[1] meets the current constraints and environmental conditions. For example, in a time-constrained situation, an agent may sacrifice solution quality, and pay a larger fee, to produce a result within the specified deadline. Detailed discussions of TÆMS are provided elsewhere (Decker and Lesser 1993; Wagner *et al.* 1998b).

For example, consider how TÆMS could be used to coordinate the tasks assigned to different departments in a hospital. The departments need to coordinate the execution of these tasks to produce maximum medical benefit to patients under time and cost constraints. For a given patient, the radiology department may wish to schedule an x-ray, the nursing staff may wish to draw blood for diagnostic tests, and the cafeteria may wish to provide breakfast for the patient. The existence of NLEs among the methods needed to complete these tasks implies a specific order of execution. For example, eating breakfast may disable some diagnostic tests and the radioactive elements ingested for some x-rays may hinder obtaining accurate results from blood tests. These constraints imply a schedule with the order: blood tests, x-rays, and breakfast.

To be more specific, Figure 1 shows a partial TÆMS task structure for the hospital agents (Decker and Li 1998) coordinating their services for a single patient. Radiology has the task of taking an x-ray of the patient. This task requires execution of three methods: providing a barium solution for the patient to ingest, producing an exposure of the patient, and interpreting the exposure. The barium solution enables the interpretation (without it the interpretation would always have zero quality) and the exposure enables the interpretation. Similarly, the nursing staff wish to conduct tests on the patient's blood. The first method of this activity, drawing blood, enables the two tests. One of the tests is hindered if the patient has ingested a barium solution. Finally, hospital policy requires that blood be drawn and barium solutions be administered when the patient has an empty stomach.

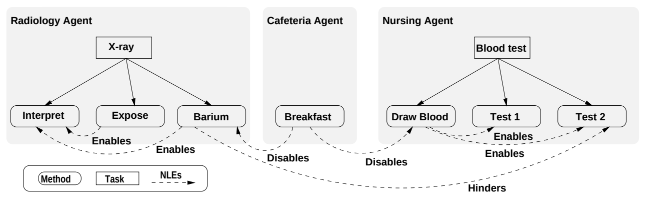


Figure 1: TÆMS Task Structure for hospital patient services.

This paper focuses on learning the statistical knowledge encoded in TÆMS about distributions and NLEs (distributions were left off figure 1 for simplicity). In particular, we focus on learning four of the most common NLEs – enables, disables, facilitates, and hinders. Each NLE defines a relation between one task or method (A) and another task or method (B). For clarity and brevity, only effects on quality are discussed; effects on duration and cost can be inferred from con-

[1]The general action selection problem in TÆMS is exponential and reasoners generally use a real-time, satisficing, goal-directed, approximation strategy (Wagner *et al.* 1998a). Thus, "best" in this case does not necessarily denote optimal.

text. Similarly, the term "precede" is used to mean that a method successfully completes execution prior the the beginning of execution for another method.

- *Enables* — If A does not precede B, then B fails, achieving a quality $q(B) = 0$. If multiple methods or tasks enable B, then *all* must precede B in order for B to be enabled.

- *Disables* — The complement of *enables.* If A precedes B, then B fails, achieving a quality $q(B) = 0$. If multiple methods or tasks disable B, then B will fail if *any* of them precede B.

- *Facilitates* — If A precedes B, then the quality of B is multiplied by a given power factor ϕ, where $\phi > 1$. That is, $q(B|A) = \phi_{AB} q(B|\overline{A})$. *Facilitates* can modify one or more performance characteristics of B. Multiple facilitating methods are multiplicative in their effects. That is, if A and B both facilitate C, and precede C in a schedule, then $q(C|AB) = \phi_{AC}\phi_{BC} q(C|\overline{AB})$.

- *Hinders* — The complement of *facilitates.* If A precedes B, then the quality of B is multiplied by a given power factor ϕ, where $\phi < 1$.

Learning Methods

Our work focuses on learning accurate knowledge of distributions and NLEs. We assume that agents already know what methods are available to be executed, and how to use TÆMS knowledge to produce effective schedules.

To learn distributions and NLEs, agents monitor the performance of schedules — finite sets of methods with at least a partial order. Each learning instance consists of the performance characteristics of a given method in the schedule (e.g., quality, duration, and cost) and the set of all methods in the schedule that successfully completed execution prior to the given method.[2] We assume that all methods in a schedule are either executed directly by the learning agent, or that the learning agent is informed of their execution. Agents are not required to infer the existence of hidden methods. Further, we assume that each schedule execution is independent; methods executed in one schedule do not affect methods executed in another schedule. This limits the scope of NLEs to methods in the schedule, consistent with the original assumptions of TÆMS.

The goal is to use learning instances to infer distributions of unaffected performance characteristics (quality, duration, and cost) for each method and to infer the existence of all NLEs and their associated power factors (ϕ). To acquire this knowledge, we built the TÆMS Learning System (TLS). TLS uses three relatively simple learning methods: 1) empirical frequency distributions; 2) deterministic properties of schedules; and 3) linear regression. Below, we discuss each method individually and discuss the interactions among the methods that allow them to be effective.

[2]From this point forward, we refer only to methods, not the more general term "methods and tasks."

Empirical frequency distributions are used to estimate distributions of performance parameters such as quality, duration, and cost. The frequency distribution for a given method and performance parameter is derived from a moving window of k instances of the execution of that method. Our goal is to estimate the distribution when *unaffected* by NLEs (i.e., the quality of method C may be affected by methods A and B that *facilitate* its execution). As a result, nearly all values are assumed to be affected by NLEs, and they are divided by the current estimates of the relevant power factors to render an estimate of the *unaffected* quality. For example, if A and B were the only methods currently thought to affect C, then $q(C|\overline{NLE}) = q(C)/(\phi_{AC}\phi_{BC})$.

An alternative approach is to learn from only those results of method executions that are guaranteed to be unaffected (e.g., the results of methods executed at the start of each schedule). In empirical tests, this approach proved far slower than the methods reported here. Figure 2 shows the results of one experiment. The top line shows the error associated with learning from only quality values guaranteed to be unaffected. The bottom line shows the error associated with learning from all values, when whose values are corrected based on estimated power factors.

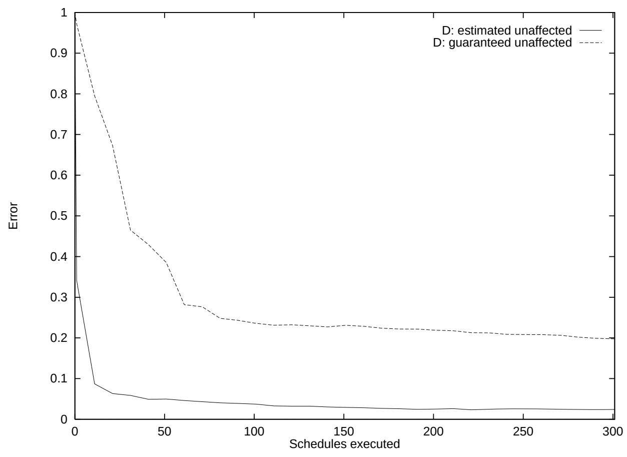


Figure 2: Error of two different methods for estimating distributions.

Deterministic properties of schedules are used to learn "hard" NLEs such as *enables* and *disables.* Although we derived a total of six such properties, two proved particularly useful in the experiments reported here. The first, *enables exclusion* states that successful execution of method A at any point in a schedule excludes all methods that did not precede A as possible enabling conditions (TÆMS requires that *all* enabling methods precede a given method for it to execute successfully). The second, *disables exclusion* states that successful execution of method A at any point in a schedule excludes all methods that precede A as possible disabling conditions (TÆMS specifies that *any* disabling method preceding a given method will disable it).

Linear regression is used to infer the existence of "soft" NLEs and to estimate their associated power factors (ϕ). Recall the TÆMS specification of how *facilitates* and *hinders* affect the performance characteristics of methods. For example, the quality of a given method m_0 is determined by its unaffected quality ($q(m_0|\overline{NLE})$) and the power factors of methods that facilitate or hinder it (e.g., m_1, m_2, and m_3). Given these NLEs, TÆMS specifies that:

$$q(m_0) = {\phi_1}^{x_1} {\phi_2}^{x_2} {\phi_3}^{x_3} q(m_0|\overline{NLE})$$

where $x_n = 1$ when m_n precedes m_0 and $x_n = 0$ otherwise. Taking the log of both sides:

$$\begin{aligned} log(q(m_0)) &= log(\phi_1)x_1 + log(\phi_2)x_2 + \\ &\quad log(\phi_3)x_3 + log(q(m_0|\overline{NLE})) \end{aligned}$$

This equation is in the classic form of a linear regression equation: $y = \beta_1 x_1 + \beta_2 x_2 + \beta_3 x_3 + \beta_0 + \epsilon$, where y corresponds to the log of the affected quality and β_1, β_2, and β_3 correspond to the logs of the respective power factors. β_0 and ϵ combine to correspond to the unaffected quality distribution, where β_0 is the distribution's mean and ϵ corresponds to the random deviations of its values from that mean.

To find NLEs affecting each method, we search for equations containing power factors ϕ that are significantly different than one (represented by regression coefficients β significantly different from zero). We conduct this search using a standard statistical method, stepwise linear regression (Draper and Smith 1981; J. Neter 1990). Stepwise regression conducts a simple local search over possible regression equations, starting with an equation containing only β_0 and ending with an equation containing at most k terms, where k is the number of methods available in each schedule. Terms are added to the equation if their coefficients are significantly different than one, and are removed if their coefficients are not significantly different than one (coefficients of existing terms in an equation can change when new terms are added).

Three assumptions of linear regression create potential problems for applying the technique to learn power factors for soft NLEs. Under the first assumption, independence of the variables x_n, knowing a value of one x should tell us nothing about the value of any other x. Unfortunately, hard NLEs can cause successful execution of some methods to be dependent on the successful execution of others, introducing dependence among the variables x_n. The NLE A *enables* B introduces a positive correlation between x_A and x_B; A *disables* B introduces a negative correlation. Regression is robust against moderate violations of this assumption, but strong violations can greatly increase the variance of estimated coefficients of the regression equation (in our case, causing the estimates of power factors to be extremely inflated or deflated). TLS addresses this problem in two ways. First, it checks for strong violations of this assumption (often referred to as perfect multicollinearity), and doesn't alter the current state of knowledge in such cases. In our experiments, such violations typically occurred only in very small datasets. Second, TLS uses *stepwise* regression which greatly reduces the total number of variables in regression equations, thus reducing the probability that two or more of them will be dependent.

Under the second assumption, normally-distributed errors, the distribution of the error term in the regression equation should be normal. In our case, the error term represents the log of the unaffected quality distribution $log(q(m_0|\overline{NLE}))$ (shifted so its mean is zero). To match this assumption, the distribution itself should be log-normal. While this is one reasonable quality distribution, it is not the only reasonable one. We experiment with an alternative distribution to indicate how linear regression is robust to moderate violations of this assumption.

The third assumption affects how we test statistical significance. Such tests are run to determine which coefficients β differ significantly from zero. The stringency of any one test is determined by α_1, which indicates the probability of a Type I error (incorrectly rejecting the null hypothesis that a single coefficient is zero). However, for a single performance parameter (e.g., quality) and k methods in a schedule, $k(k-1)$ possible NLEs exist. TLS tests whether each of these NLEs exists. Under these conditions, the probability of TLS making at least one Type I error is much larger than α_1. If the NLEs are independent, the probability is:

$$\alpha_{\text{TLS}} = 1 - (1 - \alpha_1)^{k(k-1)}$$

For example, for the overall probability of error α_{TLS} to be small (e.g., 0.10) in our base case experiment, the probability of error on any one test α_1 must be much smaller (0.000012). This process is called *Bonferroni adjustment.* Some such adjustment is important in any context where many explicit or implicit hypothesis tests are made (Jensen and Cohen 1999). TLS uses Bonferroni adjustment to set appropriate values of α_1 so that α_{TLS} is small.

Experiments

We measure the effectiveness of TLS with metrics that directly measure the quality of the learned knowledge, rather than indirectly measuring its effect on agent coordination. This approach focuses evaluation on TLS and avoids confounding TLS' performance with the performance of other system components for scheduling and coordination (Wagner *et al.* 1997). However, it could also inappropriately credit or penalize TLS for learning knowledge that is unimportant or infrequently used, respectively. To guard against this latter error, we review the utility of the learned knowledge at the the next section and show that the most useful knowledge is generally learned most quickly.

In each experiment, agents create learning data by generating and executing schedules. In all experiments reported here, agents operate in an exploration mode, executing randomly-generated schedules, rather than attempting to use already learned knowledge to generate maximally effective schedules. In practice, agents are likely to mix exploration and exploitation of learned knowledge, and even to use directed exploration. These options will be explored in later work.

Agents have access to performance parameters of executed schedules — values of quality, duration, and cost for each method in a schedule — that are affected by an initially unknown set of NLEs. The actual unaffected distributions and NLEs are hidden from agents, but they determine the values of performance parameters observed by agents.

Consistent with other projects using TÆMS, we use discrete probability distributions. However, our methods for learning hard and soft NLEs apply equally well to cases with continuous probability distributions, and a method such as kernel density estimators (John and Langley 1995) could be used to estimate continuous probability distributions from empirical data.

The experiments were conducted in two phases. First, a base case was run with settings corresponding to the assumptions of the learning techniques, particularly linear regression. Second, those settings were systematically altered to test the effects of violations of those assumptions. For the base case, schedules contain 30 unique methods, executed in a random order. Method performance is controlled by a TÆMS task structure containing 15 NLEs (three disables, four enables, four facilitates, and four hinders). In addition, the task structure avoids cases where a single method is affected by more than one NLE. Values of ϕ for the soft NLEs deviate moderately from unity (3.0 for facilitate and 0.5 for hinders). The discrete probability distributions for performance parameters of methods (e.g., quality) are approximately log-normal. To learn empirical frequency distributions, TLS uses a window size of 100, and to learn soft NLEs, it uses $\alpha_{\text{TLS}} = 0.10$. In the next section, we show results for this base case, and results for dependent NLEs, log-uniform quality distributions, soft NLEs with small deviations from unity, and a larger number of soft NLEs.

To measure learning in TLS, we use four error metrics, each of which applies to one of the three pairs of learning methods and learned knowledge. TLS' error in learning distributions with empirical frequencies is measured by the mean difference in areas ($\overline{D}$) between the cumulative probability plots of the actual and learned distributions. For example, figure 3 shows how D is calculated for a method in a particularly simple case. D is normalized by dividing by the total range of the quality ($q_{max} - q_{min}$) so that it varies between 0 and 1. The mean of D, $\overline{D}$, measures the average D across all methods.

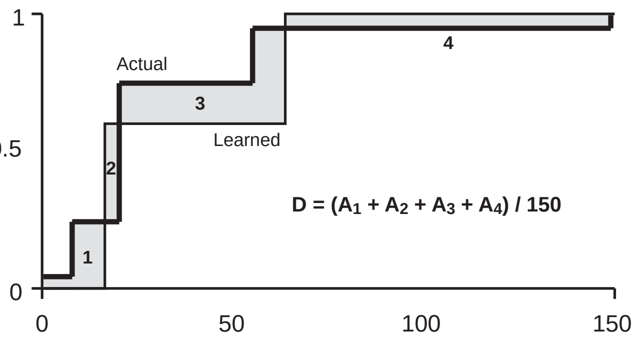


Figure 3: Difference in cumulative probability between learned and actual distributions

TLS' error in learning hard NLEs with deterministic properties is measured by the proportion of misclassified hard NLEs (H). All experiments reported in this paper begin with the assumption that all possible hard NLEs exist — a total of $k(k-1)$ possible hard NLEs among k methods. Deterministic properties are then used to eliminate hard NLEs until only true ones remain. The deterministic properties used by TLS are guaranteed to preserve actual hard NLEs, thus H always measures the extra NLEs that the system was unable to eliminate from consideration.

TLS' error in learning soft NLEs with stepwise linear regression is measured by two different metrics. The first measures the errors in TLS' inferences about *which* soft NLEs exist; the second measures the errors in TLS' estimates of the *power factors* for inferred NLEs. The first metric, S, is the proportion of all true soft NLEs that are learned correctly (*number of soft NLEs learned / number of true soft NLEs*). In the base case used in the experiments, there are eight soft NLEs. The second metric, $\overline{\delta}$, is the average difference between the actual power factor and the learned power factor. For a given soft NLE i, $\delta = |\phi_{i_{actual}} - \phi_{i_{learned}}|$). The mean difference, $\overline{\delta}$, measures the average δ across all possible soft NLEs.

Results

Figure 5a shows the values of the first three error metrics (excluding $\overline{\delta}$) for the base conditions (the settings outlined above). In fewer than 100 schedules, the distributions and hard NLEs are learned with low error. TLS continues to reduce the number of spurious hard NLEs, reaching one by the time 300 schedules are executed. The existence of all soft NLEs is not correctly inferred until more than 240 schedules have been executed, although all but one is inferred in less than 150 schedules.

To explore the robustness of TLS, we tested four alternatives to the base conditions: 1) dependent NLEs rather than independent NLEs; 2) log-uniform quality distributions rather than log-normal; 3) $\phi_{facilitates} = 1.5$ and $\phi_{hinders} = 0.75$ rather than $\phi_{facilitates} = 3.0$ and $\phi_{hinders} = 0.5$; and 4) 15 soft NLEs rather than 8 soft and 7 hard.

Figure 5b shows the sum of the errors in the power factors, δ, for the base conditions and all four alternative conditions. All tend toward zero as the number of schedule executions increases, but the base conditions cause the fastest convergence. Decreasing the deviations of the power factors from one causes a long plateau before sufficient data accumulate to begin learning these small deviations. Similarly, dependence among the NLEs also causes a plateau, because the hard NLEs prevent some methods from executing, depriving the regression of the data needed to infer soft NLEs. A log-uniform distribution causes larger errors in power factors.

One result that figures 5a and b do not convey clearly is the degree to which distributions are learned correctly. Figure 4 shows a cumulative probability plot comparing an actual distribution and a learned distribution for a method affected by a single *hinders* under the base conditions. The plot shows the distribution after 300 schedules. The learned distribution closely approximates the actual distribution.

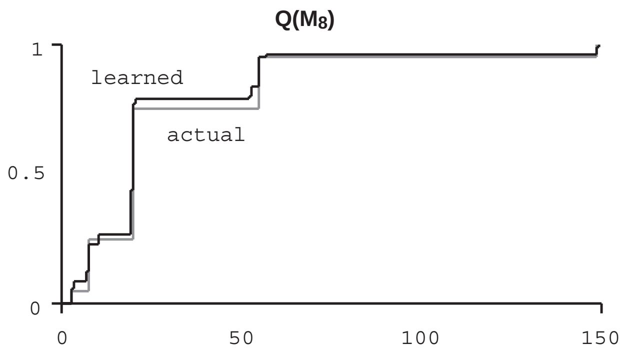


Figure 4: Cumulative probability plot of actual and learned distributions of quality

Figures 5c-f show the same content as figure 5a, but for the four alternative conditions outlined above. In these alternative conditions, distributions and hard NLEs are still learned very rapidly, but the speed with which soft NLEs can be inferred is generally reduced.

The experiments revealed some unexpected difficulties in learning. For example, the overall low error rate for NLEs masks some subtle limitations that prevents TLS from accurately learning all NLEs when such relationships are dependent (e.g., Figure 5c). The situation shown in figure 6 demonstrates three cases of such limitations. The *disables* between M_1 and M_3 is spurious, but cannot be eliminated. For any schedule in which M_1 precedes M_3, M_3 will be disabled because of the valid hard NLEs connecting M_1, M_2, and M_3, thus simulating a *disables* between M_1 and M_3. For the same reason, the *hinders* between M_1 and M_3 cannot be learned. Finally, the spurious *disables* between M_1 and M_2 cannot be eliminated because the valid *enables* NLE between the two methods prevents M_1 from every preceding M_2. Fortunately, much of the knowledge made inaccessible by these limitations concerns "impossible schedules" — schedules that could never be executed in practice. However, future versions of TLS will account for this minor pathology.

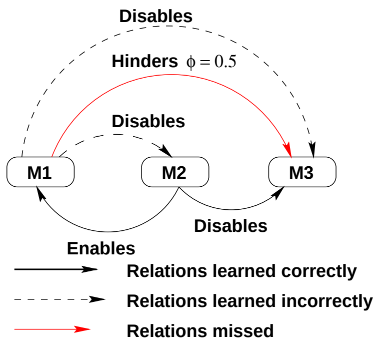


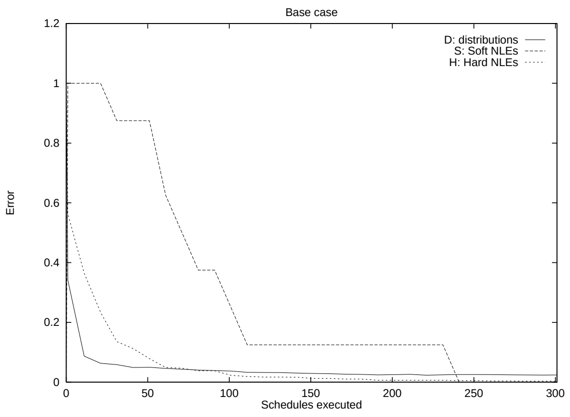
Figure 6: Dependent NLEs that prevent learning

The error graphs in figure 5 also indicate how the most important coordination knowledge is often learned most quickly. For example, TLS learns large power factors more quickly than small factors, and it learns hard NLEs (e.g., *enables* and *disables*) much more quickly than soft NLEs. Though not shown in experiments, empirical probability distributions learn the probabilities of the most frequent values of distributions most rapidly.

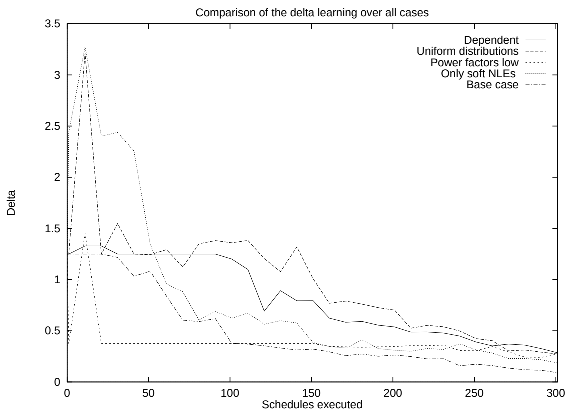
Conclusions

Our results indicate that TLS is relatively robust and can learn hard NLEs and method distributions from a small number of schedule executions, often less than 50 schedules. TLS can infer the existence of soft NLEs and their associated power factors, although this requires a moderately larger number of schedules.

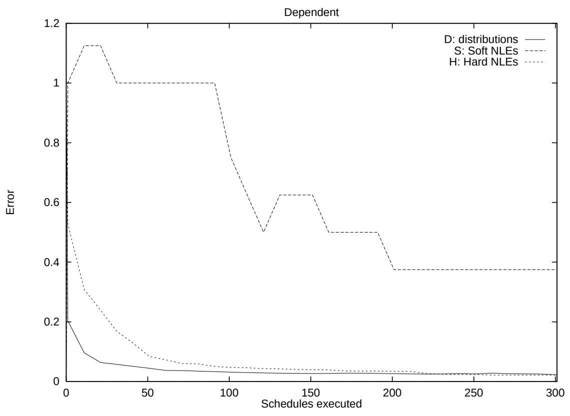
These learned NLEs may act among the local methods of one agent, or methods in several different agents (as indicated in the hospital scheduling example). Although we experiment with a single agent learning quantitative coordination knowledge, TLS is fully able to learn NLEs across multiple agents if each agent has access to the schedule and execution characteristics of methods. We have already designed a distributed version of TLS, where each agent exchanges executed schedules for learning. In this design, we can have several agents using TLS to learn only those NLEs that affect their own methods or one dedicated learning agent that learns for the whole community.



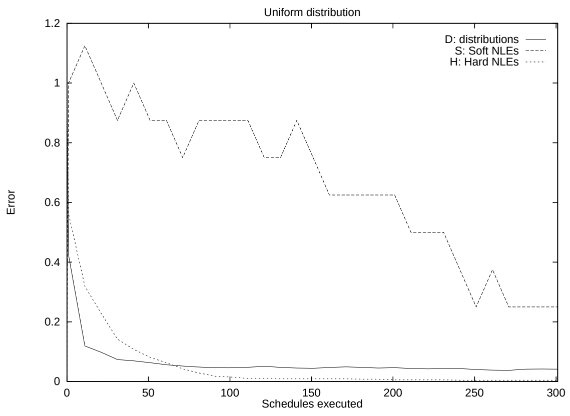
a) Base case results



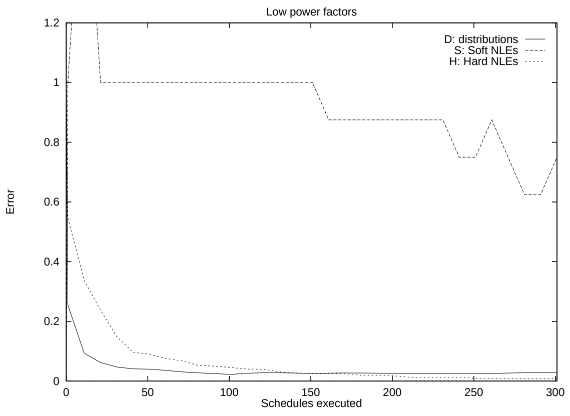
b) Average error in power factor (δ) for all 5 cases.



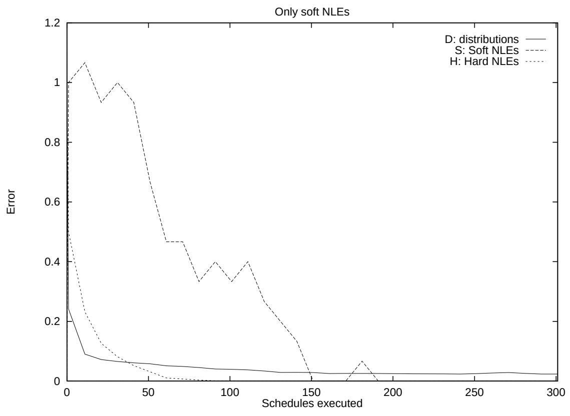
c) Dependent NLEs



d) Log-uniform distributions



e) Small deviations in power factors



f) Only soft NLEs

Figure 5: Errors for learning hard NLEs, soft NLEs, and method distributions under different conditions

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